

Name: _____

Dr. Jay H. Baltisberger

Please answer 5 of 6 questions, showing all calculations - 35 points each, 175 total.

- Briefly explain why the hydrogen atom wavefunction solutions are not exact for a helium atom.
- Given the term symbol 2P for a sodium atom in an excited state ($1s^2 2s^2 2p^6 4p^1$), explain the meaning of the superscript 2 and the P. How many distinct types of wavefunctions would the 2P term symbol allow in this case? Calculate the orbital angular momentum for this term symbol.
- When doing a numerical calculation of the wavefunctions for a given atom, a common approach is called the Hartree-Fock (HF) self-consistent field (SCF) method. Describe how this approach is used to generate ground state wavefunctions and energies for a given atom.
- Write the Slater determinant for the ground state wavefunction of a boron atom (B, 5 electrons). Use the notation $1s_{A \uparrow}$, $2s_{B \downarrow}$, $3p_{C \uparrow}$, etc. for the electrons labeled A through E, where \uparrow and \downarrow are the spin portion of the wavefunction for each electron. Explain how this determinant relates to the Pauli principle and anti-symmetry of the wavefunction.
- For a hydrogen atom, calculate the radius (r_{2s}) at which the probability of finding the electron in then enclosed region is 90%. For hydrogen, $Z = 1$ and $a = 0.5295 \times 10^{-8}$ cm. For a spherical integral, $d\tau = r^2 \sin \theta dr d\theta d\phi$.

$$\Psi_{2s} = (1/4) (2/a)^{-1/2} (Z/a)^{3/2} (2 - Zr/a) e^{-Zr/2a}$$

- Recall that when adding spin and orbital angular momenta to arrive at a total electronic angular momentum J, we use the sum $J = |L + S|, |L + S - 1|, \dots, |L - S|$. What are possible J values for each of the following term symbols: 4P , 3D and 2S .