

**Examination 1**  
**Chemistry 262**

**October 13, 1993**  
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Name: \_\_\_\_\_

1. What, specifically, leads to quantization of energy levels in the harmonic oscillator problem?  
(15 points)

2. Which of the following two functions is an eigenfunction of the momentum operator and what is the eigenvalue for this function? (20 points)

$$\hat{p}_x = \frac{\hbar}{i} \frac{d}{dx}$$

$$\psi_1 = A \exp(-ikx)$$

$$\psi_2 = Ax \exp(-kx^2) + B \exp(-kx^2)$$

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3. Which of the following functions can not be a real world wavefunction and why? (15 points)

$$\psi_1 = \frac{A}{x} \exp(-ix) \quad \psi_2 = A|x| \quad \psi_3 = \begin{cases} A \exp(x) & x < 0 \\ 2A \exp(-ikx) & x > 0 \end{cases}$$

4. How would you calculate the mean square position expectation value for the second excited state particle in a box. (20 points, 5 Bonus points if you perform integration using the integral provided)

$$\psi_n = \frac{1}{\sqrt{L}} \cos \frac{n\pi x}{2L} \quad \int x^2 \cos^2 x \, dx = \frac{x^3}{6} + \frac{2x^2 - 1}{8} \sin 2x + \frac{x \cos 2x}{4} + C$$

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5. What is the energy for a particle with the wavefunction below in a one dimensional harmonic oscillator potential. (5 points for setting up derivatives, 5 points for actually performing the correct differentiation, 5 Bonus points for setting the additional calculation of the mean square momentum of this state)

$$\psi_1 = N_2 \frac{4x^2}{\alpha^2} - 2 \exp\left(-x^2/2\alpha^2\right) \quad \alpha^2 = \hbar/m\omega \quad \hat{H} = \frac{-\hbar^2}{2m} \frac{d^2}{dx^2} + \frac{m\omega^2 x^2}{2}$$

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6. Draw pictorially the wavefunctions for particles with the energy levels indicated below ( $E_1$  and  $E_2$ ) for the following potential. Notice that energy state  $E_1$  is less than the middle potential  $V_2$  but larger than the other two potentials  $V_1$  and  $V_3$ . Energy state  $E_2$  on the other hand is larger than  $V_1$ ,  $V_2$  and  $V_3$ . Indicate where the wavelength of the wavefunction will be largest and smallest. Also, indicate where the wavefunction has a sinusoidal form and where it has an exponential form. (20 points)

